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Title Site Percolation on Square Lattices (SPSL)

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Description Provides basic functionality for labeling iso- & anisotropic percolation clusters on 2D & 3D square lattices with various lattice sizes, occupation probabilities, von Neumann & Moore (1,d)-neighborhoods, and random variables weighting the percolation lattice sites.

Depends stats

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SPSL-package	<i>Site Percolation on Square Lattices (SPSL)</i>
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Description

Provides basic functionality for labeling iso- & anisotropic percolation clusters on 2D & 3D square lattices with various lattice sizes, occupation probabilities, von Neumann & Moore (1,d)-neighborhoods, and random variables weighting the percolation lattice sites.

Details

Package:	SPSL
Type:	Package
Version:	0.1-9
Date:	2019-03-17
License:	GPL-3
LazyLoad:	yes

`ssi20()` and `ssi30()` functions provide sites labeling of the isotropic cluster on 2D & 3D square lattice with von Neumann (1,0)-neighborhood.

`ssa20()` and `ssa30()` functions provide sites labeling of the anisotropic cluster on 2D & 3D square lattice with von Neumann (1,0)-neighborhood.

`ssi2d()` and `ssi3d()` functions provide sites labeling of the isotropic cluster on 2D & 3D square lattice with Moore (1,d)-neighborhood.

`ssa2d()` and `ssa3d()` functions provide sites labeling of the anisotropic cluster on 2D & 3D square lattice with Moore (1,d)-neighborhood.

`fssi20()` and `fssi30()` functions calculates the relative frequency distribution of isotropic clusters on 2D & 3D square lattice with von Neumann (1,0)-neighborhood.

`fssa20()` and `fssa30()` functions calculates the relative frequency distribution of anisotropic clusters on 2D & 3D square lattice with von Neumann (1,0)-neighborhood.

`fssi2d()` and `fssi3d()` functions calculates the relative frequency distribution of isotropic clusters on 2D & 3D square lattice with Moore (1,d)-neighborhood.

`fssa2d()` and `fssa3d()` functions calculates the relative frequency distribution of anisotropic clusters on 2D & 3D square lattice with Moore (1,d)-neighborhood.

Author(s)

Pavel V. Moskalev <moskaleff@gmail.com>

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2014) Estimates of threshold and strength of percolation clusters on square lattices with (1,d)-neighborhood. *Computer Research and Modeling*, Vol.6, No.3, pp.405–414; in Russian.
- [3] Moskalev, P.V. (2013) The structure of site percolation models on three-dimensional square lattices. *Computer Research and Modeling*, Vol.5, No.4, pp.607–622; in Russian.

fssa20

Frequency of Sites on a Square Anisotropic 2D lattice with (1,0)-neighborhood

Description

fssa20() function calculates the relative frequency distribution of anisotropic clusters on 2D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
fssa20(n=1000, x=33, p=runif(4, max=0.9),
      set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 2D square percolation lattice.
p	a vector of relative fractions ($0 < p_i < 1$) of accessible sites (occupation probability) for lattice directions: (-x, +x, -y, +y).
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites and the vector p , distributed over the lattice directions.

The anisotropic cluster is formed from the accessible sites connected with the initial subset set , and depends on the direction in 2D square lattice.

Von Neumann (1,0)-neighborhood on 2D square lattice consists of sites, only one coordinate of which is different from the current site by one: $e=c(-1, 1, -x, x)$.

Each element of the matrix rfq is equal to the relative frequency with which the 2D square lattice site belongs to a cluster sample of size n .

Value

rfq a 2D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskaleff@gmail.com>

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[ssa20](#), [fssa30](#), [fssi20](#), [fssi30](#), [fssa2d](#), [fssa3d](#)

Examples

```
x <- y <- seq(33)
image(x, y, rfq <- fssa20(n=200, p=c(.3,.4,.75,.5)), cex.main=1,
main="Frequencies of anisotropic (1,0)-clusters")
contour(x, y, rfq, levels=seq(.2,.3,.05), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssa2d

Frequency of Sites on a Square Anisotropic 2D lattice with (1,d)-neighborhood

Description

`fssa2d()` function calculates the relative frequency distribution of anisotropic clusters on 2D square lattice with Moore (1,d)-neighborhood.

Usage

```
fssa2d(n=1000, x=33,
      p0=runif(4, max=0.8),
      p1=colMeans(matrix(p0[c(1,3, 2,3, 1,4, 2,4)], nrow=2))/2,
      set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 2D square percolation lattice.
p0	a vector of relative fractions ($0 < p_0 < 1$) of accessible sites (occupation probability) for lattice directions: (-x, +x, -y, +y).
p1	averaged double combinations of p0-components weighted by Minkowski distance: $p_1 = \text{colMeans}(\text{matrix}(p_0[c(1,3, \dots)], \text{nrow}=2)) / \rho_M e_1$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites and the vectors p0 and p1, distributed over the lattice directions, and their combinations.

The anisotropic cluster is formed from the accessible sites connected with the initial subset set, and depends on the direction in 2D square lattice.

Moore (1,d)-neighborhood on 2D square lattice consists of sites, at least one coordinate of which is different from the current site by one: $e = c(e_0, e_1)$, where

```
e0=c(-1, 1, -x, x);
```

```
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4)], nrow=2)).
```

Minkowski distance between sites a and b depends on the exponent d:

```
rhoM <- function(a, b, d=1)
```

```
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
```

```
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from e1 subset with the exponent d=1 is equal to $\rho_M e_1 = 2$.

Each element of the matrix frq is equal to the relative frequency with which the 2D square lattice site belongs to a cluster sample of size n.

Value

frq a 2D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskaleff@gmail.com>

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[ssa2d](#), [fssa3d](#), [fssa20](#), [fssa30](#), [fssi2d](#), [fssi3d](#)

Examples

```
x <- y <- seq(33)
image(x, y, rfq <- fssa2d(n=200, p0=c(.3,.4,.75,.5)), cex.main=1,
main="Frequencies of anisotropic (1,1)-clusters")
contour(x, y, rfq, levels=seq(.2,.3,.05), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssa30	<i>Frequency of Sites on a Square Anisotropic 3D lattice with (1,0)-neighborhood</i>
--------	--

Description

`fssa30()` function calculates the relative frequency distribution of anisotropic clusters on 3D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
fssa30(n=1000, x=33, p=runif(6, max=0.6),
      set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 3D square percolation lattice.
p	a vector of relative fractions ($0 < p_i < 1$) of accessible sites (occupation probability) for lattice directions: $(-x, +x, -y, +y, -z, +z)$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if <code>all=TRUE</code> , mark all sites from a starting subset; if <code>all=FALSE</code> , mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites and the vector p , distributed over the lattice directions.

The anisotropic cluster is formed from the accessible sites connected with the initial subset set , and depends on the direction in 3D square lattice.

Von Neumann (1,0)-neighborhood on 3D square lattice consists of sites, only one coordinate of which is different from the current site by one: $e=c(-1, 1, -x, x, -x^2, x^2)$.

Each element of the 3D matrix rfq is equal to the relative frequency with which the 3D square lattice site belongs to a cluster sample of size n .

Value

rfq a 3D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskalefff@gmail.com>

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[ssa30](#), [fssa20](#), [fssi20](#), [fssi30](#), [fssa2d](#), [fssa3d](#)

Examples

```
x <- y <- seq(33)
rfq <- fssa30(n=200, p=.17*c(.5,3,.5,1.5,1,.5))
image(x, y, rfq[, ,17], cex.main=1,
main="Frequencies in z=17 slice of anisotropic (1,0)-clusters")
contour(x, y, rfq[, ,17], levels=seq(.05,.3,.05), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssa3d

Frequency of Sites on a Square Anisotropic 3D lattice with (1,d)-neighborhood

Description

`fssa3d()` function calculates the relative frequency distribution of anisotropic clusters on 3D square lattice with Moore (1,d)-neighborhood.

Usage

```
fssa3d(n=1000, x=33,
      p0=runif(6, max=0.4),
      p1=colMeans(matrix(p0[c(
        1,3, 2,3, 1,4, 2,4,
        1,5, 2,5, 1,6, 2,6,
        3,5, 4,5, 3,6, 4,6)], nrow=2))/2,
      p2=colMeans(matrix(p0[c(
        1,3,5, 2,3,5, 1,4,5, 2,4,5,
        1,3,6, 2,3,6, 1,4,6, 2,4,6)], nrow=3))/3,
      set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 2D square percolation lattice.
p0	a vector of relative fractions ($0 < p_0 < 1$) of accessible sites (occupation probability) for lattice directions: (-x, +x, -y, +y, -z, +z).
p1	averaged double combinations of p0-components weighted by Minkowski distance: $p_1 = \text{colMeans}(\text{matrix}(p_0[c(1,3, \dots)], \text{nrow}=2)) / \text{rhoMe1}$.
p2	averaged triple combinations of p0-components weighted by Minkowski distance: $p_2 = \text{colMeans}(\text{matrix}(p_0[c(1,3,5, \dots)], \text{nrow}=3)) / \text{rhoMe2}$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites acc and the vectors p0, p1, and p2, distributed over the lattice directions, and their combinations.

The anisotropic cluster is formed from the accessible sites connected with the initial subset set, and depends on the direction in 3D square lattice.

Moore (1,d)-neighborhood on 3D square lattice consists of sites, at least one coordinate of which is different from the current site by one: $e = c(e_0, e_1, e_2)$, where

```
e0=c(-1, 1, -x, x, -x^2, x^2);
```

```
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4, 1,5, 2,5, 1,6, 2,6, 3,5, 4,5, 3,6, 4,6)],
nrow=2));
```

```
e2=colMeans(matrix(p0[c(1,3,5, 2,3,5, 1,4,5, 2,4,5, 1,3,6, 2,3,6, 1,4,6, 2,4,6)],
nrow=3)).
```

Minkowski distance between sites a and b depends on the exponent d:

```
rhoM <- function(a, b, d=1)
```

```
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
```

```
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```


Minkowski distance for sites from e1 and e2 subsets with the exponent $d=1$ is equal to $\rho_{Me1}=2$ and $\rho_{Me2}=3$.

Each element of the matrix `rfq` is equal to the relative frequency with which the 3D square lattice site belongs to a cluster sample of size n .

Value

`rfq` a 3D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskalefff@gmail.com>

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[ssa3d](#), [fssa2d](#), [fssa20](#), [fssa30](#), [fssi2d](#), [fssi3d](#)

Examples

```
x <- y <- seq(33)
rfq <- fssa3d(n=200, p0=.17*c(.5,3,.5,1.5,1,.5))
image(x, y, rfq[, ,17], cex.main=1,
main="Frequencies in z=17 slice of anisotropic (1,1)-clusters")
contour(x, y, rfq[, ,17], levels=seq(.05,.3,.05), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssi20	<i>Frequency of Sites on a Square Isotropic 2D lattice with (1,0)-neighborhood</i>
--------	--

Description

`fssi20()` function calculates the relative frequency distribution of isotropic clusters on 2D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
fssi20(n=1000, x=33, p=0.592746,
set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 2D square percolation lattice.
p	the relative fractions ($0 < p < 1$) of accessible sites (occupation probability) for percolation lattice.
set	a vector of linear indexes of a starting sites subset.
all	logical; if <code>all=TRUE</code> , mark all sites from a starting subset; if <code>all=FALSE</code> , mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites and the constant parameter p .

The isotropic cluster is formed from the accessible sites connected with initial sites subset `set`.

Von Neumann (1,0)-neighborhood on 2D square lattice consists of sites, only one coordinate of which is different from the current site by one: $e=c(-1, 1, -x, x)$.

Each element of the matrix `rfq` is equal to the relative frequency with which the 2D square lattice site belongs to a cluster sample of size n .

Value

`rfq` a 2D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2014) Estimates of threshold and strength of percolation clusters on square lattices with (1,d)-neighborhood. *Computer Research and Modeling*, Vol.6, No.3, pp.405–414; in Russian.

See Also

[ssi20](#), [fssi30](#), [fssa20](#), [fssa30](#), [fssi2d](#), [fssi3d](#)

Examples

```
x <- y <- seq(33)
image(x, y, rfq <- fssi20(n=200), cex.main=1,
main="Frequencies of isotropic (1,0)-clusters")
contour(x, y, rfq, levels=seq(.2,.3,.05), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssi2d	<i>Frequency of Sites on a Square Isotropic 2D lattice with (1,d)-neighborhood</i>
--------	--

Description

fssi2d() function calculates the relative frequency distribution of isotropic clusters on 2D square lattice with Moore (1,d)-neighborhood.

Usage

```
fssi2d(n=1000, x=33, p0=0.5, p1=p0/2,
       set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 2D square percolation lattice.
p0	a relative fraction ($0 < p0$) & ($p0 < 1$) of accessible sites (occupation probability) for percolation lattice.
p1	p0 value, weighted by Minkowski distance: $p1 = p0 / \text{rhoMe1}$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites and the constant parameters p0 and p1.

The isotropic cluster is formed from the accessible sites connected with initial sites subset set.

Moore (1,d)-neighborhood on 2D square lattice consists of sites, at least one coordinate of which is different from the current site by one: $e = c(e0, e1)$, where

```
e0=c(-1, 1, -x, x, -x^2, x^2);
e1=colSums(matrix(e0[c(1,3,2,3,1,4,2,4)], nrow=2)).
```

Minkowski distance between sites a and b depends on the exponent d:

```
rhoM <- function(a, b, d=1)
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from e1 subset with the exponent d=1 is equal to rhoMe1=2.

Each element of the matrix frq is equal to the relative frequency with which the 2D square lattice site belongs to a cluster sample of size n.

Value

rfq a 2D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskalefff@gmail.com>

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
 [2] Moskalev, P.V. (2014) Estimates of threshold and strength of percolation clusters on square lattices with (1,d)-neighborhood. *Computer Research and Modeling*, Vol.6, No.3, pp.405–414; in Russian.

See Also

[ssi2d](#), [fssi3d](#), [fssi20](#), [fssi30](#), [fssa2d](#), [fssa3d](#)

Examples

```
x <- y <- seq(33)
image(x, y, rfq <- fssi2d(n=200), cex.main=1,
main="Frequencies of isotropic (1,1)-clusters")
contour(x, y, rfq, levels=seq(.2,.3,.05), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssi30	<i>Frequency of Sites on a Square Isotropic 3D lattice with (1,0)-neighborhood</i>
--------	--

Description

fssi30() function calculates the relative frequency distribution of isotropic clusters on 3D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
fssi30(n=1000, x=33, p=0.311608,
      set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 3D square percolation lattice.
p	the relative fractions ($0 < p < 1$) of accessible sites (occupation probability) for percolation lattice.

set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites and the constant parameter p .

The isotropic cluster is formed from the accessible sites connected with initial sites subset set.

Von Neumann (1,0)-neighborhood on 3D square lattice consists of sites, only one coordinate of which is different from the current site by one: $e=c(-1, 1, -x, x, -x^2, x^2)$.

Each element of the matrix `rfq` is equal to the relative frequency with which the 3D square lattice site belongs to a cluster sample of size n .

Value

`rfq` a 3D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskaleff@gmail.com>

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[ssi30](#), [fssi20](#), [fssa20](#), [fssa30](#), [fssi2d](#), [fssi3d](#)

Examples

```
x <- y <- seq(33)
rfq <- fssi30(n=200, p=0.37)
image(x, y, rfq[, ,17], cex.main=1,
main="Frequencies in the z=17 slice of isotropic (1,0)-clusters")
contour(x, y, rfq[, ,17], levels=c(0.2,0.25,0.3), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

fssi3d *Frequency of Sites on a Square Isotropic 3D lattice with (1,d)-neighborhood*

Description

fssi3d() function calculates the relative frequency distribution of isotropic clusters on 3D square lattice with Moore (1,d)-neighborhood.

Usage

```
fssi3d(n=1000, x=33, p0=0.2, p1=p0/2, p2=p0/3,
       set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

n	a sample size.
x	a linear dimension of 3D square percolation lattice.
p0	a relative fraction ($0 < p0$) & ($p0 < 1$) of accessible sites (occupation probability) for percolation lattice.
p1	p0 value, weighted by Minkowski distance: $p1 = p0 / \text{rhoMe1}$.
p2	p0 value, weighted by Minkowski distance: $p2 = p0 / \text{rhoMe2}$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites and the constant parameters p0, p1, and p2.

The isotropic cluster is formed from the accessible sites connected with initial sites subset set.

Moore (1,d)-neighborhood on 3D square lattice consists of sites, at least one coordinate of which is different from the current site by one: $e = c(e0, e1, e2)$, where

```
e0=c(-1, 1, -x, x, -x^2, x^2);
```

```
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4, 1,5, 2,5, 1,6, 2,6, 3,5, 4,5, 3,6, 4,6)],
nrow=2));
```

```
e2=colMeans(matrix(p0[c(1,3,5, 2,3,5, 1,4,5, 2,4,5, 1,3,6, 2,3,6, 1,4,6, 2,4,6)],
nrow=3)).
```

Minkowski distance between sites a and b depends on the exponent d:

```
rhoM <- function(a, b, d=1)
```

```
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
```

```
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from e_1 and e_2 subsets with the exponent $d=1$ is equal to $\rho_{Me1}=2$ and $\rho_{Me2}=3$.

Each element of the matrix rfq is equal to the relative frequency with which the 3D square lattice site belongs to a cluster sample of size n .

Value

rfq a 3D matrix of relative sampling frequencies for sites of the percolation lattice.

Author(s)

Pavel V. Moskalev <moskaleff@gmail.com>

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[ssi3d](#), [fssi2d](#), [fssi20](#), [fssi30](#), [fssa2d](#), [fssa3d](#)

Examples

```
x <- y <- seq(33)
rfq <- fssi3d(n=200, p0=.285)
image(x, y, rfq[, ,17], cex.main=1,
main="Frequencies in the z=17 slice of isotropic (1,1)-clusters")
contour(x, y, rfq[, ,17], levels=c(0.2,0.25,0.3), add=TRUE)
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssa20

Site cluster on Square Anisotropic 2D lattice with (1,0)-neighborhood

Description

`ssa20()` function provides sites labeling of the anisotropic cluster on 2D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
ssa20(x=33, p=runif(4, max=0.9),
      set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

x	a linear dimension of 2D square percolation lattice.
p	a vector of relative fractions ($0 < p_i < 1$) of accessible sites (occupation probability) for lattice directions: $(-x, +x, -y, +y)$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites `acc` and the vector `p`, distributed over the lattice directions.

The anisotropic cluster is formed from the accessible sites connected with the initial subset, and depends on the direction in 2D square lattice.

To form the cluster the condition `acc[set+e[n]] < p[n]` is iteratively tested for sites of the von Neumann (1,0)-neighborhood `e` for the current cluster perimeter `set`, where `n` is equal to direction in 2D square lattice.

Von Neumann (1,0)-neighborhood on 2D square lattice consists of sites, only one coordinate of which is different from the current site by one: `e=c(-1, 1, -x, x)`.

Forming cluster ends with the exhaustion of accessible sites in von Neumann (1,0)-neighborhood of the current cluster perimeter.

Value

<code>acc</code>	an accessibility matrix for 2D square percolation lattice: if <code>acc[e] < p[n]</code> then <code>acc[e]</code> is accessible site; if <code>acc[e] == 1</code> then <code>acc[e]</code> is non-accessible site; if <code>acc[e] == 2</code> then <code>acc[e]</code> belongs to a sites cluster.
------------------	---

Author(s)

Pavel V. Moskalev

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[fssa20](#), [ssa30](#), [ssi20](#), [ssi30](#), [ssa2d](#), [ssa3d](#)

Examples

```
set.seed(20120507)
x <- y <- seq(33)
image(x, y, ssa2d(), zlim=c(0,2),
main="Anisotropic (1,0)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssa2d

*Site cluster on Square Anisotropic 2D lattice with (1,d)-neighborhood***Description**

ssa2d() function provides sites labeling of the anisotropic cluster on 2D square lattice with Moore (1,d)-neighborhood.

Usage

```
ssa2d(x=33, p0=runif(4, max=0.8),
      p1=colMeans(matrix(p0[c(
        1,3, 2,3, 1,4, 2,4)], nrow=2))/2,
      set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

x	a linear dimension of 2D square percolation lattice.
p0	a vector of relative fractions ($0 < p_0$) & ($p_0 < 1$) of accessible sites (occupation probability) for lattice directions: (-x, +x, -y, +y).
p1	averaged double combinations of p0-components weighted by Minkowski distance: $p_1 = \text{colMeans}(\text{matrix}(p_0[c(1,3, \dots)], \text{nrow}=2)) / \rho_{\text{Me}1}$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites acc and the vectors p0 and p1, distributed over the lattice directions, and their combinations.

The anisotropic cluster is formed from the accessible sites connected with the initial subset set, and depends on the direction in 2D square lattice.

To form the cluster the condition $\text{acc}[\text{set} + e_N[n]] < p_N[n]$ is iteratively tested for sites of the Moore (1,d)-neighborhood eN for the current cluster perimeter set, where eN is equal to e0 or e1 vector; pN is equal to p0 or p1 vector; n is equal to direction in 2D square lattice.

Moore (1,d)-neighborhood on 2D square lattice consists of sites, at least one coordinate of which is different from the current site by one: $e=c(e_0, e_1)$, where

```
e0=c(-1, 1, -x, x);
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4)], nrow=2)).
```

Minkowski distance between sites a and b depends on the exponent d:

```
rhoM <- function(a, b, d=1)
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from e1 subset with the exponent d=1 is equal to $\rho_M e_1 = 2$.

Forming cluster ends with the exhaustion of accessible sites in Moore (1,d)-neighborhood of the current cluster perimeter.

Value

acc an accessibility matrix for 2D square percolation lattice:
if $\text{acc}[e] < pN[n]$ then $\text{acc}[e]$ is accessible site;
if $\text{acc}[e] == 1$ then $\text{acc}[e]$ is non-accessible site;
if $\text{acc}[e] == 2$ then $\text{acc}[e]$ belongs to a sites cluster.

Author(s)

Pavel V. Moskalev

References

[1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.

See Also

[fssa2d](#), [ssa3d](#), [ssa20](#), [ssa30](#), [ssi2d](#), [ssi3d](#)

Examples

```
set.seed(20120507)
x <- y <- seq(33)
image(x, y, ssa2d(), zlim=c(0,2),
main="Anisotropic (1,1)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssa30

Site cluster on Square Anisotropic 3D lattice with (1,0)-neighborhood

Description

`ssa30()` function provides sites labeling of the anisotropic cluster on 3D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
ssa30(x=33, p=runif(6, max=0.6),
      set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

x	a linear dimension of 3D square percolation lattice.
p	a vector of relative fractions ($0 < p_i < 1$) of accessible sites (occupation probability) for lattice directions: $(-x, +x, -y, +y, -z, +z)$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if <code>all=TRUE</code> , mark all sites from a starting subset; if <code>all=FALSE</code> , mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites `acc` and the vector `p`, distributed over the lattice directions.

The anisotropic cluster is formed from the accessible sites connected with the initial subset `set`, and depends on the direction in 3D square lattice.

To form the cluster the condition `acc[set+e[n]] < p[n]` is iteratively tested for sites of the von Neumann (1,0)-neighborhood `e` for the current cluster perimeter `set`, where `n` is equal to direction in 3D square lattice.

Von Neumann (1,0)-neighborhood on 3D square lattice consists of sites, only one coordinate of which is different from the current site by one: `e=c(-1, 1, -x, x, -x^2, x^2)`.

Forming cluster ends with the exhaustion of accessible sites in von Neumann (1,0)-neighborhood of the current cluster perimeter.

Value

<code>acc</code>	an accessibility matrix for 3D square percolation lattice: if <code>acc[e] < p[n]</code> then <code>acc[e]</code> is accessible site; if <code>acc[e] == 1</code> then <code>acc[e]</code> is non-accessible site; if <code>acc[e] == 2</code> then <code>acc[e]</code> belongs to a sites cluster.
------------------	---

Author(s)

Pavel V. Moskalev

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2013) The structure of site percolation models on three-dimensional square lattices. *Computer Research and Modeling*, Vol.5, No.4, pp.607–622; in Russian.

See Also

[fssa30](#), [ssa20](#), [ssi20](#), [ssi30](#), [ssa2d](#), [ssa3d](#)

Examples

```
# Example No.1. Axonometric projection of 3D cluster
require(lattice)
set.seed(20120521)
x <- y <- z <- seq(33)
cls <- which(ssa30(p=.09*c(1,6,1,3,2,1))>1, arr.ind=TRUE)
cloud(cls[,3] ~ cls[,1]*cls[,2],
      xlim=range(x), ylim=range(y), zlim=range(z),
      col=rgb(1,0,0,0.4), xlab="x", ylab="y", zlab="z", main.cex=1,
      main="Anisotropic (1,0)-cluster")

# Example No.2. Z=17 slice of 3D cluster
set.seed(20120521)
x <- y <- z <- seq(33)
cls <- ssa30(p=.09*c(1,6,1,3,2,1))
image(x, y, cls[, ,17], zlim=c(0,2), cex.main=1,
      main="Z=17 slice of an anisotropic (1,0)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

 ssa3d

Site cluster on Square Anisotropic 3D lattice with (1,d)-neighborhood

Description

ssa3d() function provides sites labeling of the anisotropic cluster on 3D square lattice with Moore (1,d)-neighborhood.

Usage

```
ssa3d(x=33, p0=runif(6, max=0.4),
      p1=colMeans(matrix(p0[c(
        1,3, 2,3, 1,4, 2,4,
        1,5, 2,5, 1,6, 2,6,
        3,5, 4,5, 3,6, 4,6)], nrow=2))/2,
      p2=colMeans(matrix(p0[c(
        1,3,5, 2,3,5, 1,4,5, 2,4,5,
        1,3,6, 2,3,6, 1,4,6, 2,4,6)], nrow=3))/3,
      set=(x^3+1)/2, all=TRUE,
      shape=c(1,1))
```

Arguments

x a linear dimension of 3D square percolation lattice.

<code>p0</code>	a vector of relative fractions ($0 < p0$) & ($p0 < 1$) of accessible sites (occupation probability) for lattice directions: (-x, +x, -y, +y, -z, +z).
<code>p1</code>	averaged double combinations of <code>p0</code> -components weighted by Minkowski distance: <code>p1=colMeans(matrix(p0[c(1,3,...)], nrow=2))/rhoMe1</code> .
<code>p2</code>	averaged triple combinations of <code>p0</code> -components weighted by Minkowski distance: <code>p2=colMeans(matrix(p0[c(1,3,5,...)], nrow=3))/rhoMe2</code> .
<code>set</code>	a vector of linear indexes of a starting sites subset.
<code>all</code>	logical; if <code>all=TRUE</code> , mark all sites from a starting subset; if <code>all=FALSE</code> , mark only accessible sites from a starting subset.
<code>shape</code>	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites `acc` and the vectors `p0`, `p1`, and `p2`, distributed over the lattice directions, and their combinations.

The anisotropic cluster is formed from the accessible sites connected with the initial subset `set`, and depends on the direction in 3D square lattice.

To form the cluster the condition `acc[set+eN[n]] < pN[n]` is iteratively tested for sites of the Moore (1,d)-neighborhood `eN` for the current cluster perimeter `set`, where `eN` is equal to `e0`, `e1`, or `e2` vector; `pN` is equal to `p0`, `p1`, or `p2` vector; `n` is equal to direction in 3D square lattice.

Moore (1,d)-neighborhood on 3D square lattice consists of sites, at least one coordinate of which is different from the current site by one: `e=c(e0, e1, e2)`, where

```
e0=c(-1, 1, -x, x, -x^2, x^2);
```

```
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4, 1,5, 2,5, 1,6, 2,6, 3,5, 4,5, 3,6, 4,6)],
nrow=2));
```

```
e2=colMeans(matrix(p0[c(1,3,5, 2,3,5, 1,4,5, 2,4,5, 1,3,6, 2,3,6, 1,4,6, 2,4,6)],
nrow=3)).
```

Minkowski distance between sites `a` and `b` depends on the exponent `d`:

```
rho.mink <- function(a, b, d=1)
```

```
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
```

```
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from `e1` and `e2` subsets with the exponent `d=1` is equal to `rhoMe1=2` and `rhoMe2=3`.

Forming cluster ends with the exhaustion of accessible sites in Moore (1,d)-neighborhood of the current cluster perimeter.

Value

<code>acc</code>	an accessibility matrix for 3D square percolation lattice: if <code>acc[e] < pN[n]</code> then <code>acc[e]</code> is accessible site; if <code>acc[e] == 1</code> then <code>acc[e]</code> is non-accessible site; if <code>acc[e] == 2</code> then <code>acc[e]</code> belongs to a sites cluster.
------------------	--

Author(s)

Pavel V. Moskalev

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2013) The structure of site percolation models on three-dimensional square lattices. *Computer Research and Modeling*, Vol.5, No.4, pp.607–622; in Russian.

See Also

[fssa3d](#), [ssa2d](#), [ssa20](#), [ssa30](#), [ssi2d](#), [ssi3d](#)

Examples

```
# Example No.1. Axonometric projection of 3D cluster
require(lattice)
set.seed(20120521)
x <- y <- z <- seq(33)
cls <- which(ssa3d(p0=.09*c(1,6,1,3,2,1))>1, arr.ind=TRUE)
cloud(cls[,3] ~ cls[,1]*cls[,2],
xlim=range(x), ylim=range(y), zlim=range(z),
col=rgb(1,0,0,0.4), xlab="x", ylab="y", zlab="z", main.cex=1,
main="Anisotropic (1,1)-cluster")

# Example No.2. Z=17 slice of 3D cluster
set.seed(20120521)
x <- y <- z <- seq(33)
cls <- ssa3d(p0=.09*c(1,6,1,3,2,1))
image(x, y, cls[, ,17], zlim=c(0,2), cex.main=1,
main="Z=17 slice of an anisotropic (1,1)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssi20

Site cluster on Square Isotropic 2D lattice with (1,0)-neighborhood

Description

`ssi20()` function provides sites labeling of the isotropic cluster on 2D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
ssi20(x=33, p=0.592746,
      set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

- `x` a linear dimension of 2D square percolation lattice.
- `p` the relative fractions ($0 < p < 1$) of accessible sites (occupation probability) for percolation lattice.

set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites `acc` and the constant parameter `p`.

The isotropic cluster is formed from the accessible sites connected with initial sites subset.

To form the cluster the condition `acc[set+e]<p` is iteratively tested for sites of the von Neumann (1,0)-neighborhood `e` for the current cluster perimeter `set`.

Von Neumann (1,0)-neighborhood on 2D square lattice consists of sites, only one coordinate of which is different from the current site by one: `e=c(-1, 1, -x, x)`.

Forming cluster ends with the exhaustion of accessible sites in von Neumann (1,0)-neighborhood of the current cluster perimeter.

Value

<code>acc</code>	an accessibility matrix for 2D square percolation lattice: if <code>acc[e]<p</code> then <code>acc[e]</code> is accessible site; if <code>acc[e]==1</code> then <code>acc[e]</code> is non-accessible site; if <code>acc[e]==2</code> then <code>acc[e]</code> belongs to a sites cluster.
------------------	--

Author(s)

Pavel V. Moskalev

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2014) Estimates of threshold and strength of percolation clusters on square lattices with (1,d)-neighborhood. *Computer Research and Modeling*, Vol.6, No.3, pp.405–414; in Russian.

See Also

[fssi20](#), [ssi30](#), [ssa20](#), [ssa30](#), [ssi2d](#), [ssi3d](#)

Examples

```
set.seed(20120507)
x <- y <- seq(33)
image(x, y, ssi20(), zlim=c(0,2),
main="Isotropic (1,0)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssi2d

*Site cluster on Square Isotropic 2D lattice with (1,d)-neighborhood***Description**

ssi2d() function provides sites labeling of the isotropic cluster on 2D square lattice with Moore (1,d)-neighborhood.

Usage

```
ssi2d(x=33, p0=0.5, p1=p0/2,
      set=(x^2+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

x	a linear dimension of 2D square percolation lattice.
p0	a relative fraction ($0 < p0$) & ($p0 < 1$) of accessible sites (occupation probability) for percolation lattice.
p1	p0 value, weighted by Minkowski distance: $p1 = p0 / \rho_M^{e1}$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 2D square lattice with uniformly weighted sites acc and the constant parameters p0 and p1.

The isotropic cluster is formed from the accessible sites connected with initial sites subset set.

To form the cluster the condition $acc[set+eN] < pN$ is iteratively tested for sites of the Moore (1,d)-neighborhood eN for the current cluster perimeter set, where eN is equal to e0 or e1 vector; pN is equal to p0 or p1 value.

Moore (1,d)-neighborhood on 2D square lattice consists of sites, at least one coordinate of which is different from the current site by one: $e=c(e0, e1)$, where

```
e0=c(-1, 1, -x, x, -x^2, x^2);
```

```
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4)], nrow=2)).
```

Minkowski distance between sites a and b depends on the exponent d:

```
rhoM <- function(a, b, d=1)
```

```
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
```

```
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from e1 subset with the exponent d=1 is equal to $\rho_M^{e1}=2$.

Forming cluster ends with the exhaustion of accessible sites in Moore (1,d)-neighborhood of the current cluster perimeter.

Value

acc an accessibility matrix for 2D square percolation lattice:
 if $\text{acc}[e] < pN$ then $\text{acc}[e]$ is accessible site;
 if $\text{acc}[e] == 1$ then $\text{acc}[e]$ is non-accessible site;
 if $\text{acc}[e] == 2$ then $\text{acc}[e]$ belongs to a sites cluster.

Author(s)

Pavel V. Moskalev <moskalefff@gmail.com>

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
 [2] Moskalev, P.V. (2014) Estimates of threshold and strength of percolation clusters on square lattices with (1,d)-neighborhood. *Computer Research and Modeling*, Vol.6, No.3, pp.405–414; in Russian.

See Also

[fssi2d](#), [ssi3d](#), [ssi20](#), [ssi30](#), [ssa2d](#), [ssa3d](#)

Examples

```
set.seed(20120507)
x <- y <- seq(33)
image(x, y, ssi2d(), zlim=c(0,2),
main="Isotropic (1,1)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssi30

Site cluster on Square Isotropic 3D lattice with (1,0)-neighborhood

Description

`ssi30()` function provides sites labeling of the isotropic cluster on 3D square lattice with von Neumann (1,0)-neighborhood.

Usage

```
ssi30(x=33, p=0.311608,
      set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

x	a linear dimension of 3D square percolation lattice.
p	the relative fractions ($0 < p < 1$) of accessible sites (occupation probability) for percolation lattice.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites acc and the constant parameter p.

The isotropic cluster is formed from the accessible sites connected with initial sites subset set.

To form the cluster the condition $acc[set+e] < p$ is iteratively tested for sites of the von Neumann (1,0)-neighborhood e for the current cluster perimeter set.

Von Neumann (1,0)-neighborhood on 3D square lattice consists of sites, only one coordinate of which is different from the current site by one: $e = c(-1, 1, -x, x, -x^2, x^2)$.

Forming cluster ends with the exhaustion of accessible sites in von Neumann (1,0)-neighborhood of the current cluster perimeter.

Value

acc	an accessibility matrix for 3D square percolation lattice: if $acc[e] < p$ then acc[e] is accessible site; if $acc[e] == 1$ then acc[e] is non-accessible site; if $acc[e] == 2$ then acc[e] belongs to a sites cluster.
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Author(s)

Pavel V. Moskalev

References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2013) The structure of site percolation models on three-dimensional square lattices. *Computer Research and Modeling*, Vol.5, No.4, pp.607–622; in Russian.

See Also

[fssi30](#), [ssi20](#), [ssa20](#), [ssa30](#), [ssi2d](#), [ssi3d](#)

Examples

```
# Example No.1. Axonometric projection of 3D cluster
require(lattice)
set.seed(20120507)
x <- y <- z <- seq(33)
cls <- which(ssi30(p=.285)>1, arr.ind=TRUE)
cloud(cls[,3] ~ cls[,1]*cls[,2],
xlim=range(x), ylim=range(y), zlim=range(z),
col=rgb(1,0,0,0.4), xlab="x", ylab="y", zlab="z", main.cex=1,
main="Isotropic (1,0)-cluster")

# Example No.2. Z=17 slice of 3D cluster
set.seed(20120507)
cls <- ssi30(p=.285)
x <- y <- z <- seq(33)
image(x, y, cls[, ,17], zlim=c(0,2), cex.main=1,
main="Z=17 slice of an isotropic (1,0)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

ssi3d

Site cluster on Square Isotropic 3D lattice with (1,d)-neighborhood

Description

ssi3d() function provides sites labeling of the isotropic cluster on 3D square lattice with Moore (1,d)-neighborhood.

Usage

```
ssi3d(x=33, p0=0.2, p1=p0/2, p2=p0/3,
      set=(x^3+1)/2, all=TRUE, shape=c(1,1))
```

Arguments

x	a linear dimension of 3D square percolation lattice.
p0	a relative fraction ($0 < p_0$) & ($p_0 < 1$) of accessible sites (occupation probability) for percolation lattice.
p1	p0 value, weighted by Minkowski distance: $p_1 = p_0 / \rho_{Me1}$.
p2	p0 value, weighted by Minkowski distance: $p_2 = p_0 / \rho_{Me2}$.
set	a vector of linear indexes of a starting sites subset.
all	logical; if all=TRUE, mark all sites from a starting subset; if all=FALSE, mark only accessible sites from a starting subset.
shape	a vector with two shape parameters of beta-distributed random variables, weighting the percolation lattice sites.

Details

The percolation is simulated on 3D square lattice with uniformly weighted sites `acc` and the constant parameters `p0`, `p1`, and `p2`.

The isotropic cluster is formed from the accessible sites connected with initial sites subset `set`.

To form the cluster the condition `acc[set+eN]<pN` is iteratively tested for sites of the Moore (1,d)-neighborhood `eN` for the current cluster perimeter `set`, where `eN` is equal to `e0`, `e1` or `e2` vector; `pN` is equal to `p0`, `p1` or `p2` value.

Moore (1,d)-neighborhood on 3D square lattice consists of sites, at least one coordinate of which is different from the current site by one: `e=c(e0,e1,e2)`, where

```
e0=c(-1, 1, -x, x, -x^2, x^2);
e1=colSums(matrix(e0[c(1,3, 2,3, 1,4, 2,4, 1,5, 2,5, 1,6, 2,6, 3,5, 4,5, 3,6, 4,6)],
nrow=2));
e2=colMeans(matrix(p0[c(1,3,5, 2,3,5, 1,4,5, 2,4,5, 1,3,6, 2,3,6, 1,4,6, 2,4,6)],
nrow=3)).
```

Minkowski distance between sites `a` and `b` depends on the exponent `d`:

```
rhoM <- function(a, b, d=1)
if (is.infinite(d)) return(apply(abs(b-a), 2, max))
else return(apply(abs(b-a)^d, 2, sum)^(1/d)).
```

Minkowski distance for sites from `e1` and `e2` subsets with the exponent `d=1` is equal to `rhoMe1=2` and `rhoMe2=3`.

Forming cluster ends with the exhaustion of accessible sites in Moore (1,d)-neighborhood of the current cluster perimeter.

Value

`acc` an accessibility matrix for 3D square percolation lattice:
if `acc[e]<pN` then `acc[e]` is accessible site;
if `acc[e]==1` then `acc[e]` is non-accessible site;
if `acc[e]==2` then `acc[e]` belongs to a sites cluster.

Author(s)

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References

- [1] Moskalev, P.V. Percolation modeling of porous structures. Moscow: URSS, 2018. 240 pp; in Russian.
- [2] Moskalev, P.V. (2013) The structure of site percolation models on three-dimensional square lattices. *Computer Research and Modeling*, Vol.5, No.4, pp.607–622; in Russian.

See Also

[fssi3d](#), [ssi2d](#), [ssi20](#), [ssi30](#), [ssa2d](#), [ssa3d](#)

Examples

```
# Example No.1. Axonometric projection of 3D cluster
require(lattice)
set.seed(20120507)
x <- y <- z <- seq(33)
cls <- which(ssi3d(p0=.285)>1, arr.ind=TRUE)
cloud(cls[,3] ~ cls[,1]*cls[,2],
xlim=range(x), ylim=range(y), zlim=range(z),
col=rgb(1,0,0,0.4), xlab="x", ylab="y", zlab="z", main.cex=1,
main="Isotropic (1,1)-cluster")

# Example No.2. Z=17 slice of 3D cluster
set.seed(20120507)
cls <- ssi3d(p0=.285)
x <- y <- z <- seq(33)
image(x, y, cls[, ,17], zlim=c(0,2), cex.main=1,
main="Z=17 slice of an isotropic (1,1)-cluster")
abline(h=17, lty=2); abline(v=17, lty=2)
```

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